BO1 History of Mathematics Lecture II Dissemination and development (AD 500 – AD 1600) Part 1: Transmission of mathematics from the ancient world

MT 2020 Week 1

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## Summary

#### Part 1

- Influence of the ancient world
- ▶ The Renaissance (15th and 16th centuries)
- The 16th century

Part 2

A case study: Napier's invention of logarithms 1614

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### Remnants of the collapse of the ancient world

- in Greek: manuscripts preserved at Constantinople and in libraries or collections around the Mediterranean
- in Latin: writings by Boethius (c. 480–524) on philosophy, arithmetic, geometry, music

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### The spread of Islam and Islamic learning

- 632–732: Islam spreads throughout Middle East, north Africa, and into Spain and Portugal
- c. 820: Bayt al-Ḥikma, the House of Wisdom, founded in Baghdad under Caliph al-Ma'mūn; it became a centre for translation into Arabic from Greek, Persian, Sanskrit
- c. 825: al-Khwārizmī active in Baghdad
- 9th century: texts on arithmetic, algebra, astronomy reach Spain

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12th century: translations from Arabic to Latin

### Oxford in the 14th century

The Merton School, a.k.a. the Merton Calculators (principally, Thomas Bradwardine, William Heytesbury, Richard Swineshead, John Dumbleton):

arithmetic using Hindu-Arabic numerals

translations of Euclid (some partial)

possibly a little algebra

computus texts (calculation of time)

astronomy and astrology

http://www.oxforddnb.com/view/theme/95034

## The mid-Renaissance (15th and 16th centuries)

Classical mathematical texts more widely available due to:

- rediscovery of manuscripts
- revival of knowledge of Greek
- (Western) invention of printing (Gutenberg, c. 1436)

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## Euclid's *Elements*: transmission history

- commentaries written by Pappus (c. AD 320), Theon (c. AD 380), Proclus (c. AD 450)
- ▶ a few propositions in Boethius (c. AD 500)
- copies in Greek (earliest from Constantinople, AD 888)
- many translations or commentaries in Arabic (AD 750–1250)
- mediaeval translations from Arabic to Latin: Adelard of Bath (1130), Robert of Chester (1145), Gerard of Cremona (mid-12th century)
- printed editions in Latin or Greek from 1482 onwards

### Euclid in Arabic

تابيت ان نَقَدِ قَطْعَ خُطُ الْطُوبَرُدَبِ سَمْعَ فللحذيق عراله الشتركعفي ودفعك چودلک مَاارَدْنَا جبذكابة المحصط متتاويد الأستخد قَالَ ثَابِتُ وَجَدِيَا فِي مِنْ الْمُتَّجَالَ: إِنَّ برمانا اخر فعوانا في الآلة الم والفطة . و بدونفش خطر د به داخه انقطة مونج مزنقج -isbeh مراجعة كالعطاد وحشاجع برزجوقاعة وَيْ مَسْرِ مَاهِ إِنْ فَأَوْ لَكَرْ نِعْظَةً مَنْزَكْرُ وَابِنَ الْجِدُفَانَ للفلكاز تراد مانقطة طاز المزخل وتصاح عتقح فزاوية درج سازاوية بزح فهمااندف

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Translated from the Greek by Ishaq ibn Hunayn, AD 1466

### Euclid I.47 from Bodleian ms. dated 888

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#### Whole manuscript is digitised: http://www.claymath.org/library/historical/euclid/

### Euclid I.47 from Bodleian ms. dated 888



http://www.claymath.org/library/historical/euclid/files/elem.1.47.html

Treatises by Archimedes: transmission history

- quoted or explained by Pappus (c. 320 AD), Theon (c. 380 AD), Eutocius (c. 520 AD)
- 6th-century Byzantine 'collected works' (Isidore of Miletus)

- several translations of individual treatises into Arabic
- translations from Arabic into Latin
- a new find in the twentieth century: www.archimedespalimpsest.org/

### Netz & Noel: The Archimedes Codex



(Weidenfeld & Nicolson, 2007)

## The Archimedes palimpsest



## The Archimedes palimpsest



Apollonius' Conics (c. 180 BC): transmission history

Books I–IV survived in Greek

Books V–VII survived only in Arabic

Book VIII is lost, known only from commentaries

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early (Latin) printed edition, 1566

(See: Mathematics emerging, §1.2.4.)

### Apollonius, Oxford, 1710



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New forces at work in the 16th century:

global exploration

growth of international commerce

 new technology (in printing, shipping, military engineering, instrumentation, etc.)

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# Simon Stevin (1548-1620), Leiden

Under the patronage of Maurice of Nassau, Prince of Orange, Stevin wrote on:

- accounting (1581)
- tables of interest (1582)
- geometry (1583)
- decimal fractions (1585)
- arithmetic (1585)
- weight and hydrostatics (1586)
- algebra (1594)
- fortification (1594)
- navigation (1599)



- mathematics (1608), including cosmography, geography, tides, heavenly motions, optics, perspective, refraction (Snell's law), pulleys, floating bodies, bookkeeping
- locks and sluices (1617)

## Thomas Harriot (1560–1621), London

Under the patronage of the Earl of Northumberland, Harriot worked on:

- navigation
- optics, refraction (Snell's law)
- rates of fall
- calculations of density
- alchemy
- geometry
- algebra
- astronomy

none of it published

Harriot papers online: http://echo.mpiwgberlin.mpg.de/content/scientific\_revolution/harriot



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