

Mathematical Institute

Generative Adversarial Networks (GANs)

THEORIES OF DEEP LEARNING: C6.5, LECTURE / VIDEO 13 Prof. Jared Tanner Mathematical Institute University of Oxford

Oxford Mathematics

Generative deep nets (Goodfellow et al. 14')

Example of a deep convolutional generator:

Generative model from 100 latent variables



128 256 512 1024 Stride 2 16 32 8 100 z Stride 2 Stride 2 Stride 2 Project and reshape CONV 1 CONV 2 CONV 3 64 CONV 4 G(z)

Figure 1: DCGAN generator used for LSUN scene modeling. A 100 dimensional uniform distribution Z is projected to a small spatial extent convolutional representation with many feature maps.

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https://arxiv.org/pdf/1511.06434.pdf
https://arxiv.org/pdf/1406.2661.pdf
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Generative deep nets (Goodfellow et al. 14')

Generative model from 100 latent variables



Train the two network parameters using the objective $\min_{G} \max_{D} n^{-1} \sum_{\mu=1}^{n} \log(D(x_{\mu}, y_{\mu})) + p^{-1} \sum_{p} \log(1 - D(G(z_{p}), y_{p}))$

Algorithm 1 Minibatch stochastic gradient descent training of generative adversarial nets. The number of steps to apply to the discriminator, k, is a hyperparameter. We used k = 1, the least expensive option, in our experiments.

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \ldots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.
- Update the discriminator by ascending its stochastic gradient:

$$abla_{ heta_d} rac{1}{m} \sum_{i=1}^m \left[\log D\left(oldsymbol{x}^{(i)}
ight) + \log \left(1 - D\left(G\left(oldsymbol{z}^{(i)}
ight)
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ight].$$

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Update the generator by descending its stochastic gradient:

$$abla_{\theta_g} rac{1}{m} \sum_{i=1}^m \log\left(1 - D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right).$$

end for

The gradient-based updates can use any standard gradient-based learning rule. We used momentum in our experiments.

https://arxiv.org/pdf/1406.2661.pdf

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Generative deep nets (Radford et al. 16')



Early training examples



Figure 2: Generated bedrooms after one training pass through the dataset. Theoretically, the model could learn to memorize training examples, but this is experimentally unlikely as we train with a small learning rate and minibatch SGD. We are aware of no prior empirical evidence demonstrating memorization with SGD and a small learning rate.

https://arxiv.org/pdf/1511.06434.pdf

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Generative deep nets (Radford et al. 16')



Later training examples



Figure 3: Generated bedrooms after five epochs of training. There appears to be evidence of visual under-fitting via repeated noise textures across multiple samples such as the base boards of some of the beds.

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Wasserstein GAN (Arjovsky et al. 17')

Optimal transport decoder



One of the central challenges with GANs is the ability to train the parameters. Improvements have been made through choice of generative architecture (DC-GAN of Radford) and through different training objective functions (W-GAN)

Algorithm 1 WGAN with gradient penalty. We use default values of $\lambda = 10$, $n_{\text{critic}} = 5$, $\alpha = 0.0001$, $\beta_1 = 0$, $\beta_2 = 0.9$.

Require: The gradient penalty coefficient λ , the number of critic iterations per generator iteration n_{critic} , the batch size m, Adam hyperparameters α, β_1, β_2 .

Require: initial critic parameters w_0 , initial generator parameters θ_0 .

1: while θ has not converged do

```
2:
              for t = 1, \dots, n_{\text{critic}} do
 3:
                     for i = 1, ..., m do
 4:
                            Sample real data x \sim \mathbb{P}_r, latent variable z \sim p(z), a random number \epsilon \sim U[0, 1].
 5:
                            \tilde{x} \leftarrow G_{\theta}(z)
                            \hat{x} \leftarrow \epsilon \hat{x} + (1 - \epsilon) \tilde{x}
 6:
                            L^{(i)} \leftarrow D_w(\tilde{\boldsymbol{x}}) - D_w(\boldsymbol{x}) + \lambda(\|\nabla_{\tilde{\boldsymbol{x}}} D_w(\hat{\boldsymbol{x}})\|_2 - 1)^2
 7:
                     end for
 8.
                     w \leftarrow \operatorname{Adam}(\nabla_w \frac{1}{m} \sum_{i=1}^m L^{(i)}, w, \alpha, \beta_1, \beta_2)
 9:
10:
              end for
              Sample a batch of latent variables \{z^{(i)}\}_{i=1}^m \sim p(z).
11:
              \theta \leftarrow \operatorname{Adam}(\nabla_{\theta} \frac{1}{m} \sum_{i=1}^{m} -D_{w}(G_{\theta}(z)), \theta, \alpha, \beta_{1}, \beta_{2})
12:
13. end while
```

https://arxiv.org/pdf/1704.00028.pdf https://arxiv.org/pdf/1701.07875.pdf

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Wasserstein GAN (Arjovsky et al. 17')

Examples of output from GAN architectures





Figure 2: Different GAN architectures trained with different methods. We only succeeded in training every architecture with a shared set of hyperparameters using WGAN-GP.

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Wasserstein GAN (Arjovsky et al. 17')

Training rate



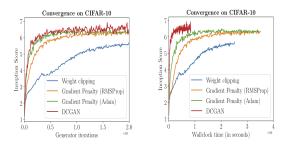


Figure 3: CIFAR-10 Inception score over generator iterations (left) or wall-clock time (right) for four models: WGAN with weight clipping, WGAN-GP with RMSProp and Adam (to control for the optimizer), and DCGAN. WGAN-GP significantly outperforms weight clipping and performs comparably to DCGAN.

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Large scale WGAN (Karras et al. 18')

Growing the encoder/decoder complexity



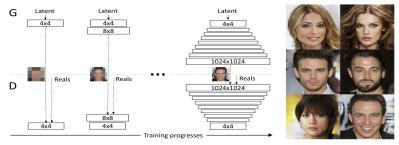


Figure 1: Our training starts with both the generator (G) and discriminator (D) having a low spatial resolution of 4×4 pixels. As the training advances, we incrementally add layers to G and D, thus increasing the spatial resolution of the generated images. All existing layers remain trainable throughout the process. Here $\boxed{N \times N}$ refers to convolutional layers operating on $N \times N$ spatial resolution. This allows stable synthesis in high resolutions and also speeds up training considerably. One the right we show six example images generated using progressive growing at 1024×1024 .

https://arxiv.org/abs/1710.10196

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Large scale WGAN (Karras et al. 18')

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Examples of synthetic faces



Figure 10: Top: Our CELEBA-HQ results. Next five rows: Nearest neighbors found from the training data, based on feature-space distance. We used activations from five VGG layers, as suggested by Chen & Koltun (2017). Only the crop highlighted in bottom right image was used for comparison in order to exclude image background and focus the search on matching facial features.

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Understanding individual units in a DNN (Bau et al. 20')

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Single units which reliably detect object classes

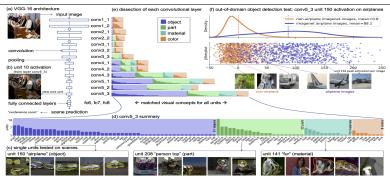


Fig. 1. The emergence of single-unit object detectors within a VGG-16 scene classifier. (a) VGG-16 consists of 13 convolutional layers, cov1_1 through coxt=3, ollowed by three fully connected layers, ccf.7, (b. (b) The activation of a single filter on a input image can be visualized as the region where the filter activates beyond its top 1% quantified level. (c) Single units are scored by matching high-activating regions against as et of human-interpretable visual concepts, each unit is labeled with its best-matching concept and visualized with maximally-activating images. (c) Concepts that matching in convolutional layer are summarized, showing a broad diversity of detectors to objects, object parts, materials, and colors. Many concepts are associated with multiple units. (e) Comparing all the layers of the network reveals that most object detectors earroge at the last convolutional layers. (f) Although the training set of challes, unit 15 de metals, unit 15 de metals, with a training and concepts activations to the unit on randomity are appled 1.00 arriginate and 1.000 non-airplane objects, as tested against a dataset of labeled object images not previously see by the network. The jitter jot shows peak activations for the unit on randomity are appled 1.00 arriginate and 1.000 non-airplane langes, and the urves show the kernel density estimates of these activations of the set of these activations.

https://arxiv.org/abs/2009.05041

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Understanding individual units in a DNN (Bau et al. 20')

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Single units which reliably generate object classes

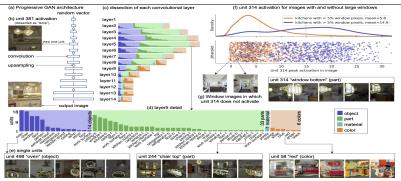


Fig. 3. The emergence of object: and part-specific units within a Progressive GAN generator(19), (a) The analyzed Progressive GAN consists of 15 convolutional layers that transform a random input vector into a synthesized image of a kitchen. (b) A single filter is visualized as the region of the output image where the filter activates beyond its top 1% quantile level; note that the filters are all precursors to the output. (c) Dissecting all the layers of the network shows a peak in object-specific units at 1_ayers 6 of the network (c) A detailed examination of 1_ayers shows more part-specific units than objects, and many visual concepts to responding to multiple units. (c) Units do not correspond to exact pixel patterns: a wide range of visual appearances for overs and chairs are generated when an oven or chair part unit are activated. (g) When a unit specific to window parts is tested as a classifier, on avonge the unit accivates more strongly on generated images that contain. larges that contain larges that contain larges that do not. (g) Some counterexamples: images for any chair on stronges to a classifier, on avonge the unit activates more stronge on to activate but where windows are synthesized nevertheles.

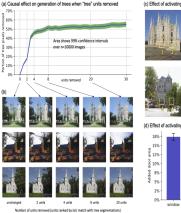
https://arxiv.org/abs/2009.05041

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Editing individual units in a DNN (Bau et al. 20')

Removing units of classes decreases their generation





(c) Effect of activating "door" units depends on location

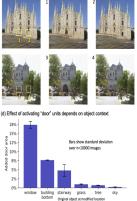


Fig. 4. The causal effect of altering units within a GAN generator. (a) When successively larger sets of units are removed from a GAN trained to generate outdoor church scenes, the tree area of the generated images is reduced. Removing 20 tree units removes more than half the generated tree pixels from the output. (b) Qualitative results: removing tree units affects trees while leaving other objects intact. Building parts that were previously occluded by trees are rendered as if revealing the objects that were behind the trees. (c) Doors can be added to buildings by activating 20 door units. The location, shape, size, and style of the rendered door depends on the location of the activated units. The same activation levels produce different doors. or no door at all (case 4) depending on locations. (d) Similar context dependence can be seen quantitatively: doors can be added in reasonable locations such as at the location of a window, but not in abnormal locations such as on a tree or in the sky.

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Adversarial Attacks for misclassification.

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Adversarial misclassification for deep nets (Goodfellow et al. 15



Imperceptible perturbation changes classification

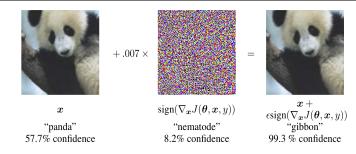


Figure 1: A demonstration of fast adversarial example generation applied to GoogLeNet (Szegedy et al.) 2014a) on ImageNet. By adding an imperceptibly small vector whose elements are equal to the sign of the elements of the gradient of the cost function with respect to the input, we can change GoogLeNet's classification of the image. Here our ϵ of .007 corresponds to the magnitude of the smallest bit of an 8 bit image encoding after GoogLeNet's conversion to real numbers.

https://arxiv.org/pdf/1412.6572.pdf

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DeepFool algorithm (Moosavi-Dezfooli et al. 15')

Many algorithms exist for computing adversarial examples



Algorithm 2 DeepFool: multi-class case

```
1:
        input: Image \boldsymbol{x}, classifier f.
        output: Perturbation \hat{r}.
  2:
 3:
        Initialize x_0 \leftarrow x, i \leftarrow 0.
  4.
        while \hat{k}(\boldsymbol{x}_i) = \hat{k}(\boldsymbol{x}_0) do
  5.
                for k \neq \hat{k}(\boldsymbol{x}_0) do
  6:
                         oldsymbol{w}_k' \leftarrow 
abla f_k(oldsymbol{x}_i) - 
abla f_{\hat{k}(oldsymbol{x}_0)}(oldsymbol{x}_i)
  7.
                        f'_k \leftarrow f_k(\boldsymbol{x}_i) - f_{\hat{h}(\boldsymbol{x}_i)}(\boldsymbol{x}_i)
  8:
                end for
  9.
               \hat{l} \leftarrow \operatorname{arg\,min}_{k \neq \hat{k}(\boldsymbol{x}_{0})} \frac{|f'_{k}|}{\|\boldsymbol{w}^{\ell}\|_{2}}
10:
               r_i \leftarrow \frac{|f_{\hat{l}}'|}{\|w'\|^2} w'_{\hat{l}}
11.
12: x_{i+1} \leftarrow \dot{x}_i + r_i
                i \leftarrow i + 1
13:
14: end while
15: return \hat{r} = \sum_i r_i
```

Alternative to Goodfellow approach of $\hat{r}(x_{\mu}) = \epsilon \operatorname{sign}(\operatorname{grad}_{x} (\theta; x_{\mu}, y_{\mu}))$. https://arxiv.org/pdf/1511.04599.pdf

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DeepFool algorithm (Moosavi-Dezfooli et al. 15')



Many algorithms exist for computing adversarial examples

Classifier	Test error	$\hat{\rho}_{adv}$ [DeepFool]	time	ρ̂ _{adv} [4]	time	ρ̂ _{adv} [18]	time
LeNet (MNIST)	1%	$2.0 imes 10^{-1}$	110 ms	1.0	20 ms	2.5×10^{-1}	>4 s
FC500-150-10 (MNIST)	1.7%	$1.1 imes 10^{-1}$	50 ms	$3.9 imes 10^{-1}$	10 ms	$1.2 imes 10^{-1}$	> 2 s
NIN (CIFAR-10)	11.5%	2.3×10^{-2}	1100 ms	$1.2 imes 10^{-1}$	180 ms	2.4×10^{-2}	>50 s
LeNet (CIFAR-10)	22.6%	$3.0 imes 10^{-2}$	220 ms	$1.3 imes 10^{-1}$	50 ms	3.9×10^{-2}	>7 s
CaffeNet (ILSVRC2012)	42.6%	$2.7 imes 10^{-3}$	510 ms*	3.5×10^{-2}	50 ms*	-	-
GoogLeNet (ILSVRC2012)	31.3%	1.9×10^{-3}	800 ms*	4.7×10^{-2}	80 ms*	-	-

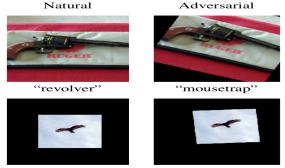
Table 1: The adversarial robustness of different classifiers on different datasets. The time required to compute one sample for each method is given in the time columns. The times are computed on a Mid-2015 MacBook Pro without CUDA support. The asterisk marks determines the values computed using a GTX 750 Ti GPU.

Average relative error of adversarial example $\hat{r}(x)$ such that $f(x) \neq f(x + \hat{r}(x))$: $\hat{\rho}_{adv}(f) = |\mathcal{D}|^{-1} \sum_{x \in \mathcal{D}} \frac{\|\hat{r}(x)\|_2}{\|x\|_2}$ https://arxiv.org/pdf/1511.04599.pdf

Rotations and Translations for CNNs (Engstrom et al. 18')



Adversarial action in space of a known invariant



"vulture"

"orangutan"

Figure 1: Examples of adversarial transformations and their predictions in the standard and "black canvas" setting.

https://arxiv.org/pdf/1712.02779.pdf

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Rotations and Translations for CNNs (Engstrom et al. 18')

Loss landscape over known invariant

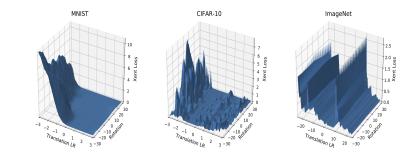


Figure 3: Loss landscape of a random example for each dataset when performing left-right translations and rotations. Translations and rotations are restricted to 10% of the image pixels and 30 deg respectively. We observe that the landscape is significantly non-concave, making rendering FO methods for adversarial example generation powerless. Additional examples are visualized in Figure 9 of the Appendix.

https://arxiv.org/pdf/1712.02779.pdf

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Universal adversary (Moosavi-Dezfooli et al. 16')



A single perturbation for many classes

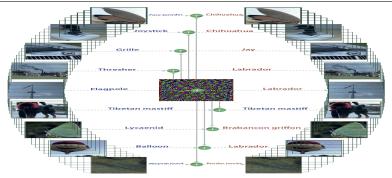


Figure 1: When added to a natural image, a universal perturbation image causes the image to be misclassified by the deep neural network with high probability. *Left images:* Original natural images. The labels are shown on top of *images*: Perturbed images. The estimated labels of the perturbed images are shown on top of each arrow.

https://arxiv.org/pdf/1610.08401.pdf

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Transferability between nets (Liu et al. 16')



Can transfer adversarial examples between nets

	RMSD	ResNet-152	ResNet-101	ResNet-50	VGG-16	GoogLeNet
-ResNet-152	17.17	0%	0%	0%	0%	0%
-ResNet-101	17.25	0%	1%	0%	0%	0%
-ResNet-50	17.25	0%	0%	2%	0%	0%
-VGG-16	17.80	0%	0%	0%	6%	0%
-GoogLeNet	17.41	0%	0%	0%	0%	5%

Table 4: Accuracy of non-targeted adversarial images generated using the optimization-based approach. The first column indicates the average RMSD of the generated adversarial images. Cell (i, j) corresponds to the accuracy of the attack generated using four models except model *i* (row) when evaluated over model *j* (column). In each row, the minus sign "–" indicates that the model of the row is not used when generating the attacks. Results of top-5 accuracy can be found in the appendix (Table 14).

RMSD is the ℓ^2 energy of the perturbation. https://arxiv.org/pdf/1611.02770.pdf

Transferability between nets (Liu et al. 16')



Can transfer adversarial examples between nets

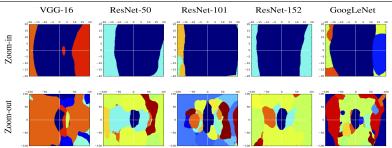


Figure 3: Decision regions of different models. We pick the same two directions for all plots: one is the gradient direction of VGG-16 (x-axis), and the other is a random orthogonal direction (y-axis). Each point in the span plane shows the predicted label of the image generated by adding a noise to the original image (e.g., the origin corresponds to the predicted label of the original image). The units of both axises are 1 pixel values. All sub-figure plots the regions on the span plane using the same label. The image is in Figure [2].

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Adversarial physical object: Turtle (Athalye et al. 17')



Physical objects can be adversarial examples: 3D

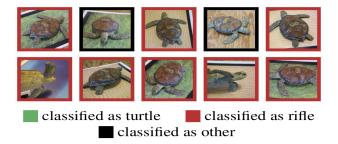


Figure 1. Randomly sampled poses of a 3D-printed turtle adversarially perturbed to classify as a rifle at every viewpoint². An unperturbed model is classified correctly as a turtle nearly 100% of the time.

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Adversarial graffiti (Eykholt et al. 17')

Physical objects can be adversarial examples: 2D





Figure 1: The left image shows real graffiti on a Stop sign, something that most humans would not think is suspicious. The right image shows our a physical perturbation applied to a Stop sign. We design our perturbations to mimic graffiti, and thus "hide in the human psyche." Table 5: A camouflage art attack on GTSRB-CNN. See example images in Table [] The targeted-attack success rate is 80% (true class label: Stop, target: Speed Limit 80).

Distance & Angle	Top Class (Confid.)	Second Class (Confid.)
5' 0°	Speed Limit 80 (0.88)	Speed Limit 70 (0.07)
5′ 15°	Speed Limit 80 (0.94)	Stop (0.03)
5′ 30°	Speed Limit 80 (0.86)	Keep Right (0.03)
5′ 45°	Keep Right (0.82)	Speed Limit 80 (0.12)
5′ 60°	Speed Limit 80 (0.55)	Stop (0.31)
10′ 0°	Speed Limit 80 (0.98)	Speed Limit 100 (0.006)
10' 15°	Stop (0.75)	Speed Limit 80 (0.20)
10' 30°	Speed Limit 80 (0.77)	Speed Limit 100 (0.11)
15′ 0°	Speed Limit 80 (0.98)	Speed Limit 100 (0.01)
15' 15°	Stop (0.90)	Speed Limit 80 (0.06)
20' 0°	Speed Limit 80 (0.95)	Speed Limit 100 (0.03)
20' 15°	Speed Limit 80 (0.97)	Speed Limit 100 (0.01)
25' 0°	Speed Limit 80 (0.99)	Speed Limit 70 (0.0008)
30′ 0°	Speed Limit 80 (0.99)	Speed Limit 100 (0.002)
40′ 0°	Speed Limit 80 (0.99)	Speed Limit 100 (0.002)

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Provable defense: convex polytope pt. 1 (Wong et al. 17)

Ensuring neighbourhood also classified correctly



Possible output of net $f_{\theta}(\cdot)$ from bounded perturbation is a non-convex set, say $\mathcal{Z}_{\epsilon}(x) = \{f_{\theta}(x + \delta) : \|\delta\|_{\infty} \leq \epsilon\}$. A convex outer-polytope of $\mathcal{Z}_{\epsilon}(x)$, say $\mathcal{Z}_{\epsilon}^{conv}(x)$, can be computed by replacing the input to each activation with a 2D convex set:

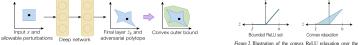


Figure 1. Conceptual illustration of the (non-convex) adversarial polytope, and an outer convex bound.

Requires knowledge of lower and upper bound for each input to a nonlinear activation. Let $c = e_{\ell} - e_{\ell'}$ or $c = 2e_{\ell} - 1_{|class|}$ and solve:

min $c^T \hat{z}_{\ell}$ and if nonnegative then robust to ϵ perturbation. $\hat{z}_{\ell} \in \hat{z}_{\epsilon}(x)$

https://arxiv.org/pdf/1711.00851.pdf

Provable defense: convex polytope pt. 2 (Wong et al. 17)

Algorithm to determine range of pre-activation values



Algorithm 1 Computing Activation Bounds

input: Network parameters $\{W_i, b_i\}_{i=1}^{k-1}$, data point x, ball size ϵ // initialization $\hat{\nu}_1 := W_1^T$ $\begin{array}{l} \gamma_1 := \gamma_1 \\ \gamma_1 := b_1^T \\ \ell_2 := x^T W_1^T + b_1^T - \epsilon \|W_1^T\|_{1,:} \\ u_2 := x^T W_1^T + b_1^T + \epsilon \|W_1^T\|_{1,:} \end{array}$ $|| \cdot ||_{1,:}$ for a matrix here denotes ℓ_1 norm of all columns for i = 2, ..., k - 1 do form $\mathcal{I}_i^-, \mathcal{I}_i^+, \mathcal{I}_i$; form D_i as in (10) // initialize new terms $\nu_{i,\mathcal{I}_i} := (D_i)_{\mathcal{I}_i} W_i^T$ $\gamma_i := b_i^T$ $\begin{array}{l} \text{''} propagate existing terms} \\ \nu_{j,\mathcal{I}_j} := \nu_{j,\mathcal{I}_j} D_i W_i^T, \quad j=2,\ldots,i-1 \\ \gamma_j := \gamma_j D_i W_i^T, \quad j=1,\ldots,i-1 \\ \tilde{\nu}_1 := \tilde{\nu}_1 D_i W_i^T \end{array}$ // compute bounds $\psi_i := x^T \hat{\nu}_1 + \sum_{i=1}^i \gamma_i$ $\ell_{i+1} := \psi_i - \epsilon \| \hat{\nu_1} \|_{1,:} + \sum_{j=2}^i \sum_{i' \in \mathcal{I}_i} \ell_{j,i'} [-\nu_{j,i'}]_+$ $u_{i+1} := \psi_i + \epsilon \|\hat{\nu}_1\|_{1,:} - \sum_{j=2}^i \sum_{i' \in \mathcal{T}_i} \ell_{j,i'} [\nu_{j,i'}]_+$ end for output: bounds $\{\ell_i, u_i\}_{i=2}^k$

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Provable defense: convex polytope pt. 3 (Wong et al. 17)

Improved robustness, but increased non-adversarial test error



Table 1. Error rates for various problems and attacks, and our robust bound for baseline and robust models.

Problem	Robust	e	TEST ERROR	FGSM error	PGD ERROR	ROBUST ERROR BOUND
MNIST	×	0.1	1.07%	50.01%	81.68%	100%
MNIST	√	0.1	1.80%	3.93%	4.11%	5.82%
Fashion-MNIST	×	0.1	9.36%	77.98%	81.85%	100%
Fashion-MNIST	√	0.1	21.73%	31.25%	31.63%	34.53%
HAR	×	0.05	4.95%	60.57%	63.82%	81.56%
HAR	√	0.05	7.80%	21.49%	21.52%	21.90%
SVHN	×	0.01	16.01%	62.21%	83.43%	100%
SVHN	√	0.01	20.38%	33.28%	33.74%	40.67%

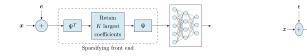
https://arxiv.org/pdf/1711.00851.pdf

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Robustness via sparsification (Gopalakrishnan et al. 18)



Removing small values improves Lipshitz constant



Sparse network

(日)

Figure 1: Sparsifying front end defense: For a basis in which the input is sparse, the input is projected onto the subspace spanned by the K largest basis coefficients. This attemates the impact of the attack by K/N, where N is the input dimension.

Figure 2: Network sparsity defense: Imposing sparsity *within* the neural network attenuates the worst-case growth of the attack as it flows up the network.

Theorem 2. Consider an ℓ_{∞} -constrained input perturbation $e_0 = e$, with $||e||_{\infty} \leq \epsilon$. Suppose that we impose ℓ_1 constraints on the weights at each layer as follows:

$$\left\|\boldsymbol{w}_{ij}\right\|_{1} \leq \gamma_{j} \ \forall \ i$$

Then the effect of the perturbation is ℓ_{∞} -bounded at each layer:

$$\left\|\boldsymbol{e}_{j}\right\|_{\infty} \leq \epsilon \prod_{l=1}^{j} \gamma_{l} \tag{2}$$

https://arxiv.org/abs/1810.10625

Robustness via sparsification (Gopalakrishnan et al. 18)



More gradual decrease in accuracy as perturbation energy increases

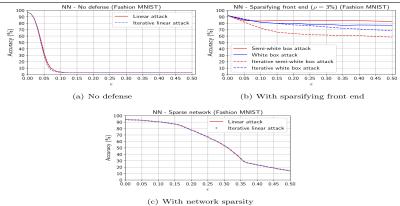


Figure 6: Fashion-MNIST: Binary classification accuracies as a function of ϵ https://arxiv.org/abs/1810.10625

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