

C5.2 Elasticity and Plasticity

Introduction to metal plasticity

By Peter Howell with minor modifications by Jim Oliver

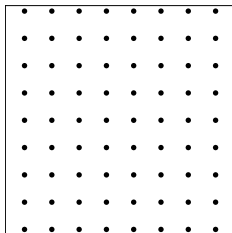
`oliver@maths.ox.ac.uk`

Michaelmas Term

Microstructure of metals

- ▶ Microstructure of metals is a periodic lattice of atoms.

- ▶ In a pristine lattice $O(1)$ strain and hence $O(\mu)$ stress required for irreversible deformation.

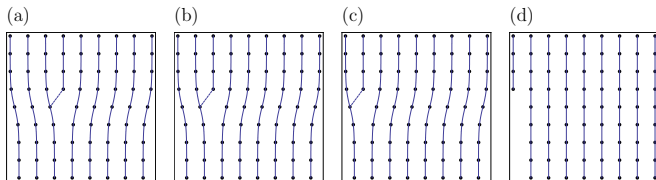


- ▶ But measured yield stresses are **much** smaller by factor of $\approx 10^{-5}$!

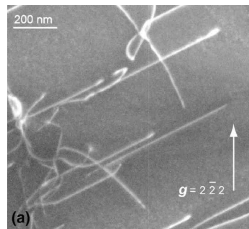
- ▶ **Hypothesis** (1930s): plastic deformation arises from motion of **dislocations**, *i.e.* crystallographic defects.

Dislocations

- ▶ Only small reorganisation of lattice is needed to shift dislocation and cause irreversible deformation of the lattice.
- ▶ For example, a moving edge dislocation:



- ▶ Requires yield stress τ_Y much smaller than μ .
- ▶ Hypothesis was confirmed **much** later by electron microscopy: metals contain trillions of dislocations which are generated and propagated by plastic deformation of the sample.



Perfect plasticity in metals

Study of behaviour of dislocations leads to the following...

Hypothesis: plastic deformation in metals is driven by **shear stress**
— normal stress does not (usually) cause irreversible deformation

Based on this hypothesis, build a **perfect plasticity** model whereby...

- ▶ $|\text{shear stress}| < \tau_Y \Rightarrow$ **elastic**
- ▶ $|\text{shear stress}| = \tau_Y \Rightarrow$ **plastic**