

# Modelling infectious disease outbreaks



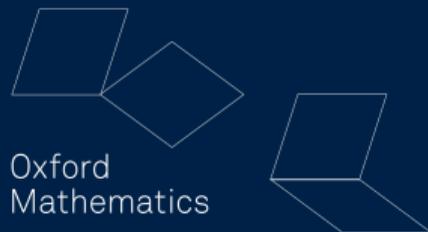
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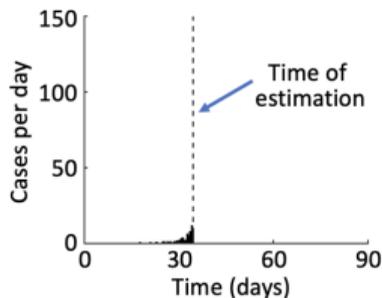
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*Mathematical Institute*

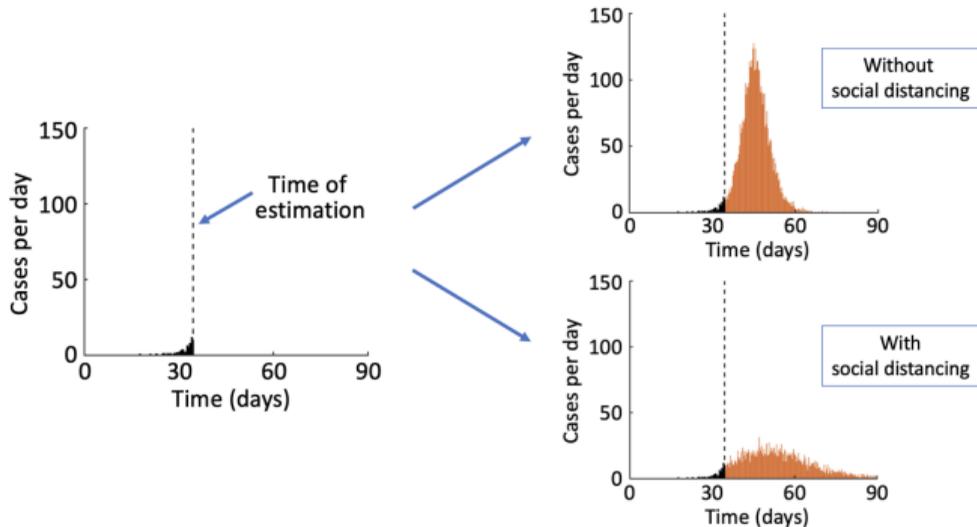
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Mathematical modelling project, Hillary term 2026





- ▶ Emerging infections require rapid and robust modelling tools.
- ▶ You will develop and analyse models to support policy decisions.



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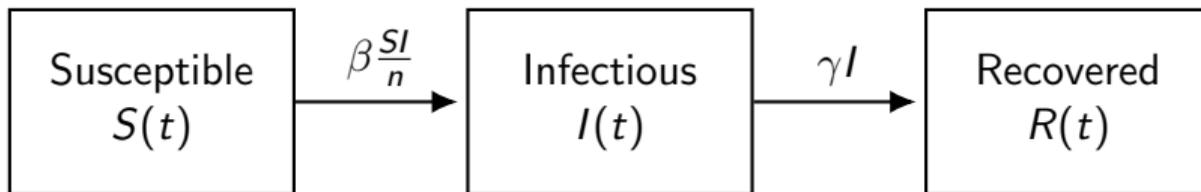
You will:

- ▶ Formulate deterministic and stochastic epidemic models.
- ▶ Fit models to outbreak data.
- ▶ Evaluate intervention strategies.

# Compartmental models (I)

The SIR epidemic model divides the population into three compartments or classes:

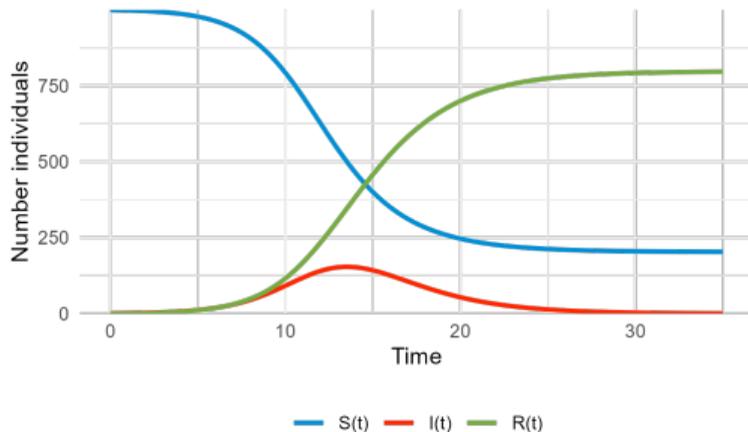
- ▶  $S$ : **susceptible** individuals who may get infected,
- ▶  $I$ : **infectious** individuals who are infected and can infect susceptible individuals,
- ▶  $R$ : **recovered** individuals who have been infected, but do no longer transmit the disease and are now immune.



# Compartmental models (II)

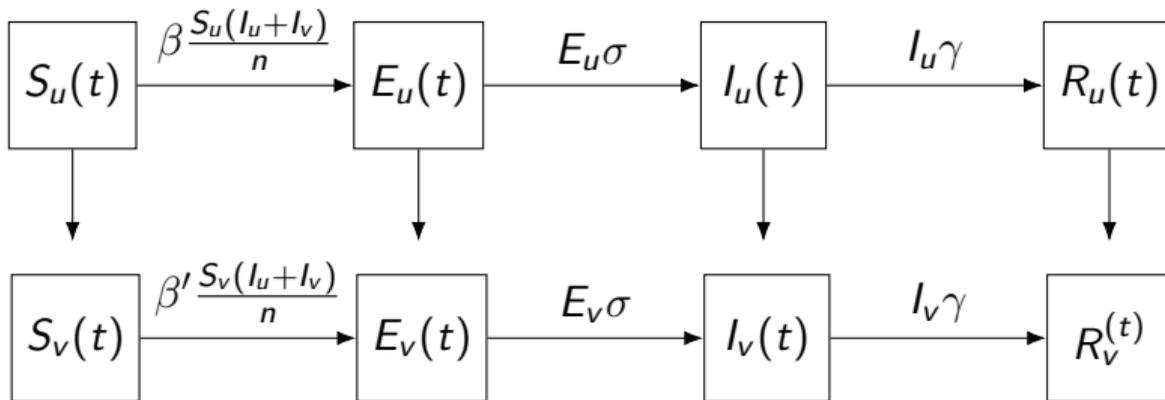
SIR model can be defined by ODEs

$$\begin{aligned}\frac{dS}{dt} &= -\beta \frac{SI}{n} \\ \frac{dI}{dt} &= \beta \frac{SI}{n} - \gamma I \\ \frac{dR}{dt} &= \gamma I\end{aligned}$$



# Compartmental models (III)

Many possible extensions including latent periods, waning immunity, or heterogeneities as age structure, vaccination status etc.

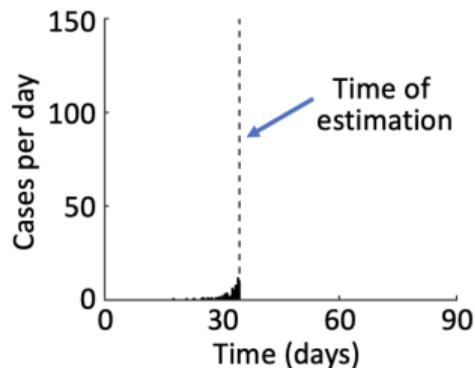


# Scenario: The OxV-26 Outbreak

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A hypothetical respiratory virus:

- ▶ Latent period:  $\sim 3$  days
- ▶ Infectious period:  $\sim 5$  days
- ▶ Asymptomatic transmission possible
- ▶ 50 initial cases, 30 days of incidence data



# Part A: Model formulation

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Core requirements:

- ▶ Deterministic SEIR model
- ▶ Stochastic model (e.g., Gillespie)

Possible extensions:

- ▶ Age structure or asymptomatic compartments
- ▶ Vaccination dynamics
- ▶ Behaviour-dependent contact rates
- ▶ Spatial or network modelling

## Part B: Parameter estimation

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You may estimate:

- ▶ Transmission rate  $\beta$
- ▶ Latent and infectious periods
- ▶ Initial conditions
- ▶  $R_0$  and  $R_t$

## Part C: Intervention strategies

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You may evaluate:

- ▶ Vaccination (efficacy, rollout speed, waning immunity)
- ▶ Testing and isolation (delays, sensitivity)
- ▶ Non-pharmaceutical interventions (mask use, distancing)
- ▶ Combinations of interventions

Goal: Identify conditions for epidemic control.

# Questions that could be addressed

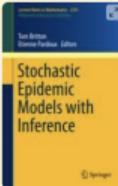
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- ▶ How do the conditions/interventions that achieve epidemic control depend on the chosen definition of “under control”?
- ▶ How does the time point at which an intervention is put into place affect its outcome?
- ▶ How do the modelling choices for any particular intervention affect the conditions for epidemic control?

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## A practical guide to mathematical methods for estimating infectious disease outbreak risks

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Suggested meeting time: Thurs 9-10 am.  
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