An 18th-century development: Newton's *Arithmetica universalis* (1707)



Rules for sums of powers of roots of

$$x^{n} - px^{n-1} - qx^{n-2} - rx^{n-3} - sx^{n-4} - \dots = 0$$

sum of roots	=	а	=	р
sum of roots ²	=	b	=	pa+2q
sum of roots ³	=	С	=	pb + qa + 3r
sum of roots ⁴	=	d	=	pc + qb + ra
sum of roots	_	u	_	pc + qb

+4s