

## A2. Metric spaces and complex analysis

Mathematical Institute, University of Oxford.

Michaelmas Term 2018

### Course information

Complex analysis is a beautiful topic and a central one in mathematics. While it builds on Prelims analysis it has a different flavour because of the richer geometry of the complex plane. It connects to many disparate parts of both pure and applied mathematics, as you will discover in a range of courses you can take later in your degree.

The first part of the course, approximately 10 lectures, is the more abstract, focusing on what are called “metric spaces”: a set equipped with a notion of distance. In this part of the course we will revisit notions you studied in Prelims Analysis, putting them into a vastly more general context. The remainder of the course will focus on the complex plane, and the study of complex-differentiable functions.

Notes for the course will be placed online in the Maths Institute Course Materials website. divided into three tranches. There will be 8 problem sets, also posted on the Course Materials website. If you spot any misprints or other errors in the online notes or problem sets please inform me via email at [mcgerty@maths.ox.ac.uk](mailto:mcgerty@maths.ox.ac.uk).

There are a number of excellent textbooks on the subject. A few of the ones you might consult include:

- *Introduction to Metric and Topological spaces*, W.A. Sutherland. O.U.P.  
*For the first part of the course on metric spaces – does all we need and much more – also useful if you take next term’s Topology course.*
- *From Real to Complex Analysis*, R. H. Dyer, D. E. Edmunds, Springer.  
*This starts with a review of the Riemann integral, and then discusses metric spaces before covering Complex Analysis. It thus follows the pattern of our course quite well.*
- *An Introduction to Complex Analysis*, H. A. Priestley. O.U.P.  
*A well-written introductory text written by one of Oxford’s own.*  
*Real and Complex Analysis*, W. A. Rudin.  
*A classic text, but rather dense and a bit more advanced in perspective than our course.*
- *Complex Analysis*, Princeton Lecture in Analysis II, E. M. Stein & R. Shakarchi. P.U.P.  
*Informally written and approachable text which covers many more topics than we will have time for.*
- *Complex Analysis*, I. Stewart, D. Tall. C.U.P.  
*Introductory text, at a similar level to Priestley.*

Note that there is a list of (very minor) corrections to the latest edition to Prof. Priestley’s book which can be found on her website, <https://people.maths.ox.ac.uk/hap>.

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